

**A. FALSE.** [A counterexample is  $X = \mathbb{B}^2$ ,  $Y = \mathbb{S}^1$ , and  $r(x, y) = (\cos 2\pi x, \sin 2\pi x)$ . If we assumed  $r$  to be a retraction, then the statement would be true.]

**B. TRUE.** [This is the lifting correspondence.]

**C. TRUE.** [Compactness guarantees that only finitely many charts (the open sets homeomorphic to open subsets of  $\mathbb{R}^n$ ) are needed to cover  $X$ . The other two conclusions are in the definition of a manifold.]

**D. FALSE.** [A counterexample is the open  $n$ -ball  $B(0, 1) \subseteq \mathbb{R}^n$ . Remember: Compactness is not about the existence of a finite open cover. Compactness is about every open cover's having a finite subcover.]

**E. TRUE.** [This  $X$  is homeomorphic to  $(0, \infty)$  by the map  $p(x, y) = x$ , and  $(0, \infty)$  is a convex subset of  $\mathbb{R}$  and hence simply connected.]